

CALCULATION POLICY

Review Due:	September 2026
Last Review	September 2024
Applicable to:	Brook Green
Reviewed by:	MW
Approved by:	SH

Rationale

This policy has been designed to teach children through the use of concrete, pictorial and abstract methods. This calculation policy should be used to support children to develop a deep understanding of number and calculation.

Policy Procedures

Using the concrete-pictorial-abstract approach:

Children develop an understanding of a mathematical concepts through the three steps (or representations), known as a concrete-pictorial-abstract approach. Reinforcement is achieved by going back and forth between these representations.

Concrete representation The enactive stage - a pupil is first introduced to an idea or a skill by acting it out with real objects. This is a 'hands on' component using real objects and it is the foundation for conceptual understanding.

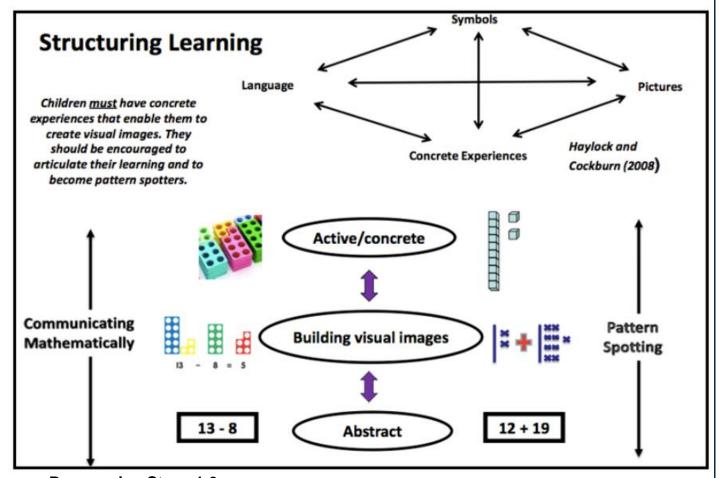
Pictorial representation The iconic stage - a pupil has sufficiently understood the hands-on experiences performed and can now relate them to representations, such as a diagram or picture of the problem.

Abstract representation The symbolic stage - a pupil is now capable of representing problems by using mathematical notation, for example: $12 \div 2 = 6$.

Guidance

This is document provides guidance and examples for key objectives for each Progression Stage but is not to be followed as a complete planning aid as not all objectives are exemplified.

B Squared continuum
Mastered
Gaining skills and understanding
Involvement
Engagement



Progression Steps 1-3

Prior to learning the following counting strategies, pupils must be secure in the 5 principles of counting (Gelman and Gallistel 1978)

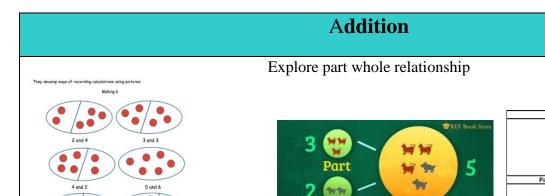
- 1. The one-one principle. I say a number for every item that I count.
- 2. The stable-order principle The number order does not change.
- 3. The cardinal principle the last number that I say describes the whole group.
- 4. The abstraction principle I can count things that I cannot touch (for example sounds)
- 5. The order-irrelevance principle It does not matter which order I count items in (link to conservation of number).

Pupils must also be confident in subitizing to 5 (recognizing small quantities without counting).

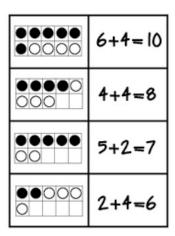
For more information on cardinality and counting, please see the following information on the NCETM website.

https://www.ncetm.org.uk/classroom-resources/ey-cardinality-and-counting/

Progression Steps 3-4



Using the ten frame to support addition of single digits – counting all/combining two groups



3 + 2

Whole

Solving problems using concrete and pictorial images.

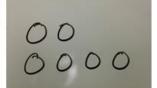
Sara has 2 apples.
Jon has 5 apples.
How many apples do
they have altogether?
How many more
apples does Jon have
than Sara?











Subtraction

Taking away after counting out practical equipment. . Children would be encouraged to physically remove these using touch counting.



By touch counting and dragging in this way, it allows children to keep track of how many they are removing so they don't have to keep recounting. They will then touch count the amount that are left to find the answer.

donut



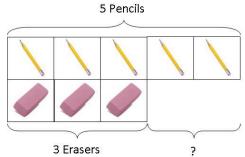


$$8 - 4 =$$

Those who are ready may record their own calculations

0 1 2 3 4 5 6 7 8 9 10

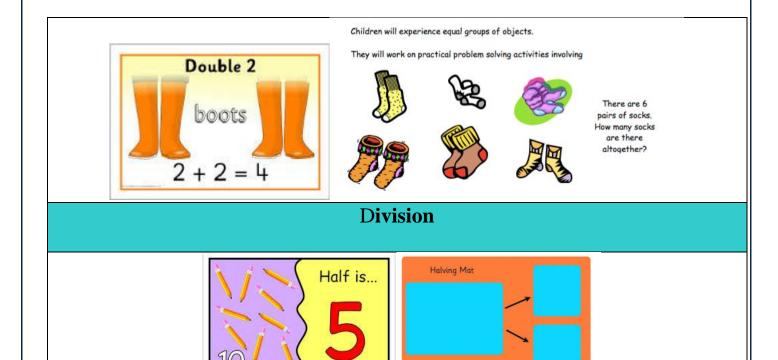
Using the ten frame to support subtraction by taking away



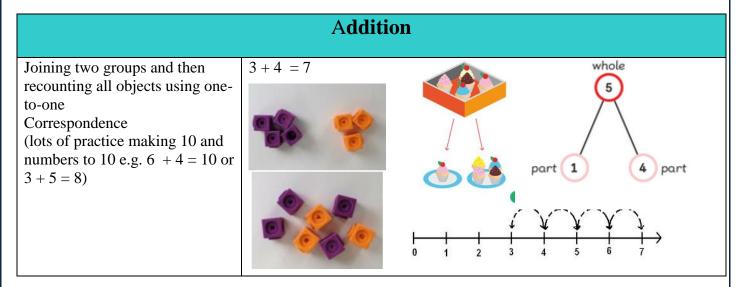
Peter has 5 pencils and 3 erasers. How many more pencils than erasers does he have? Solving problems using concrete and pictorial

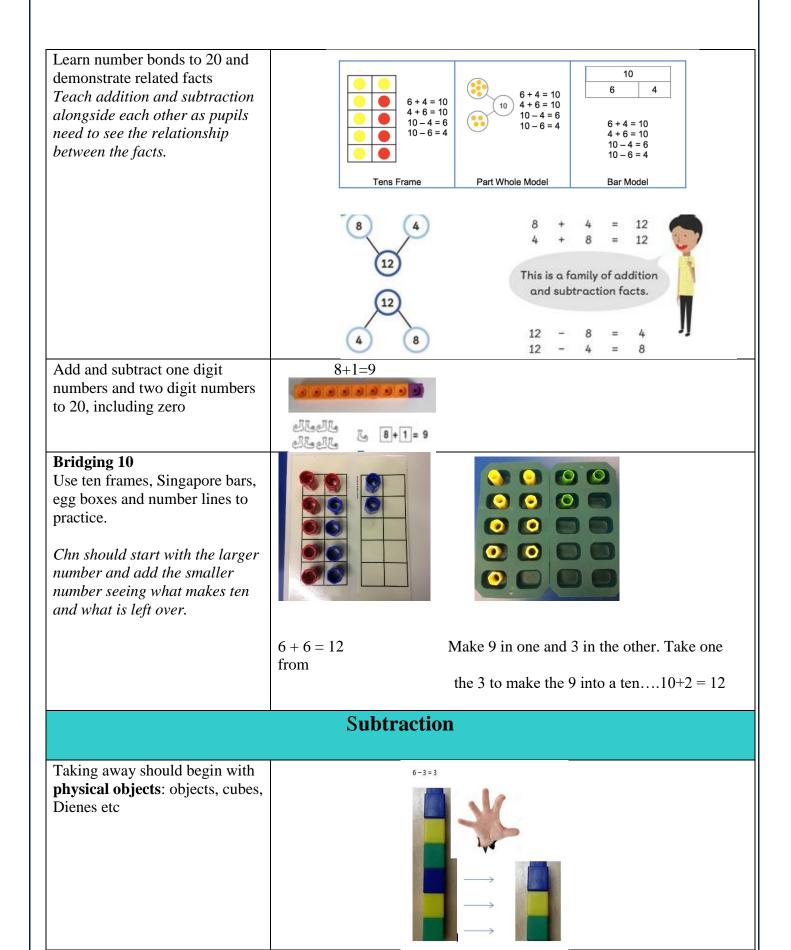
images.

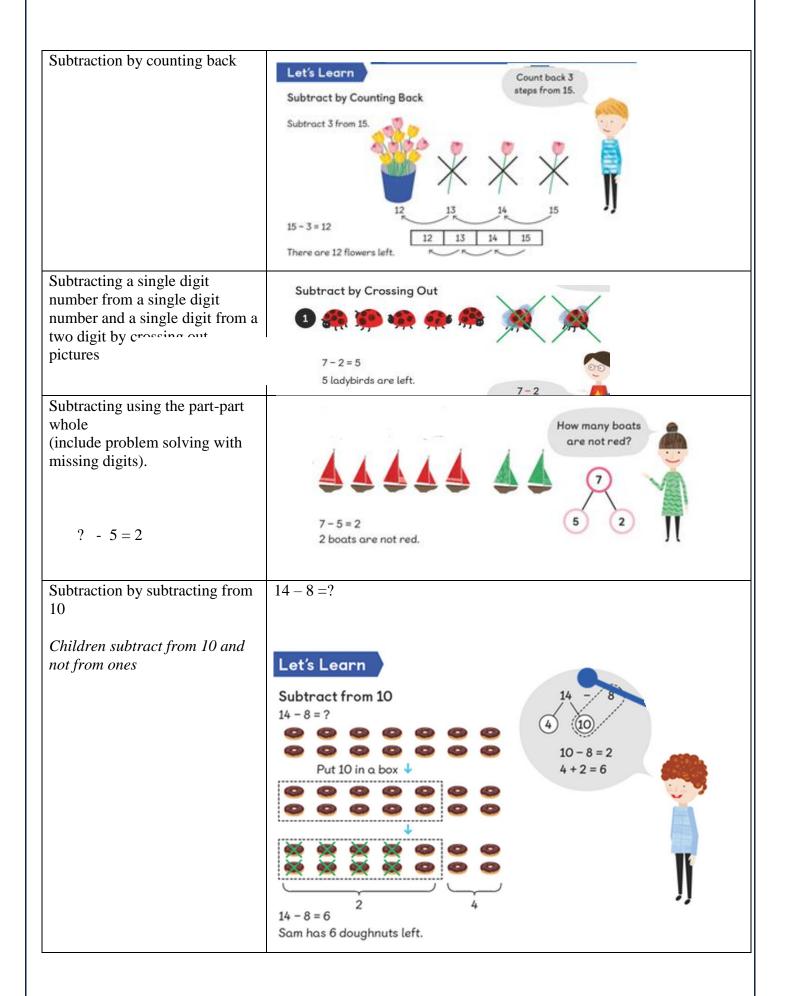
Multiplication



Progression Steps 4-6







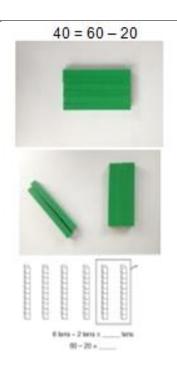
When subtracting using Dienes children should be taught to regroup a ten rod for 10 ones and then subtract from those ones

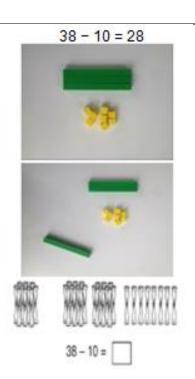


20 - 4 = 16

Subtracting multiples of 10

Using the vocabulary of 1 ten, 2 tens etc alongside 10, 20, 30 Is very important here as pupils need to understand that it is a 10 not a 1 that is being taken away





Multiplication

Counting in multiples of 2, 5 and 10 from zero

Children should count the number of groups on their fingers as they are skip counting.

2







4 groups of 2 = 8



 $2 \times 4 = 8$



2





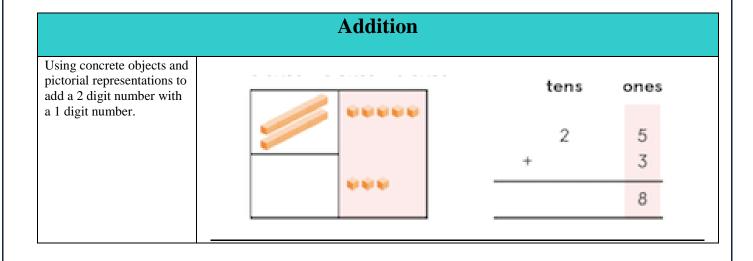
2

2

When moving to pictorial/written calculations the vocabulary is important				
	This image represents two groups of 4 or 4 twice			
Solving multiplication problems using repeated addition	3 + 3 + 3			
	How many apples are there allogether?			
	3 + 3 + 3 = 9			
	Division			
Pupils should be taught to divide through working practically and the sharing should be shown below the whole to familiarize children with the concept of the whole.	$10 \div 2 = 5$			
The language of whole and part should be used.	$8 \div 4 = 2$			
	1 There are 8 cans.			

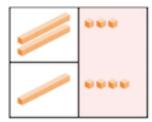
There are 4 boxes of 2 cans.

Progression Steps 5-6



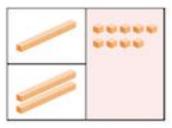
Using concrete objects and pictorial representations to add a 2 digit number and 10s number.

Step 1 Add the ones. 3 ones + 4 ones = 7 ones



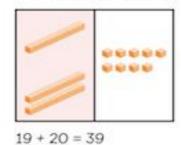
tens	ones
2 + 1	3
	7

Step 1 Add the ones.



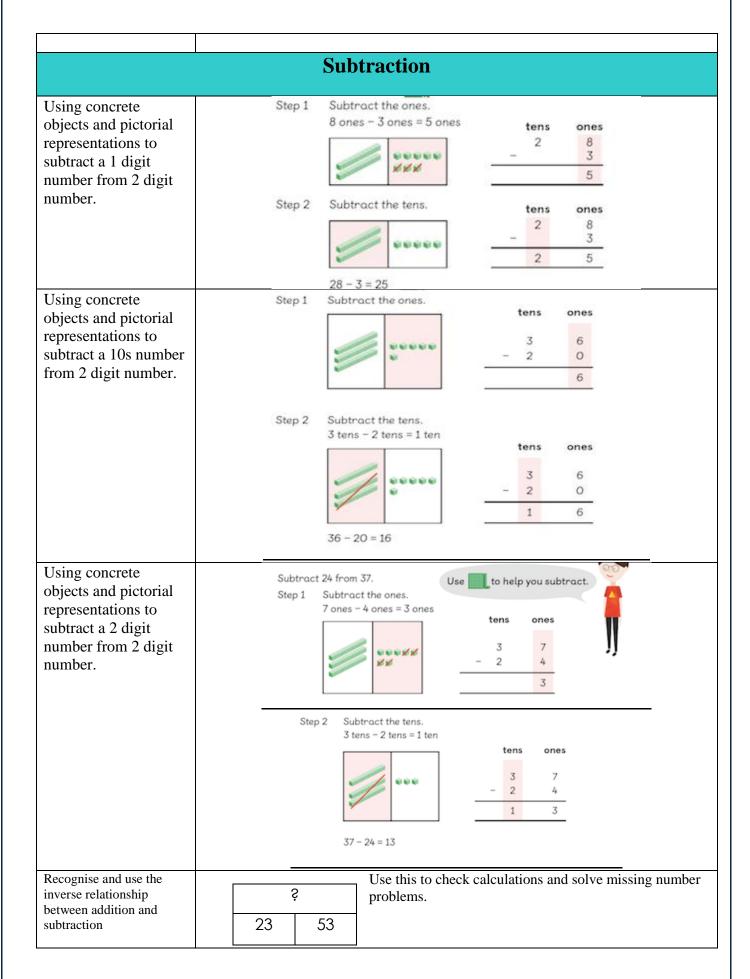
tens	ones
1	9
+ 2	0
	9

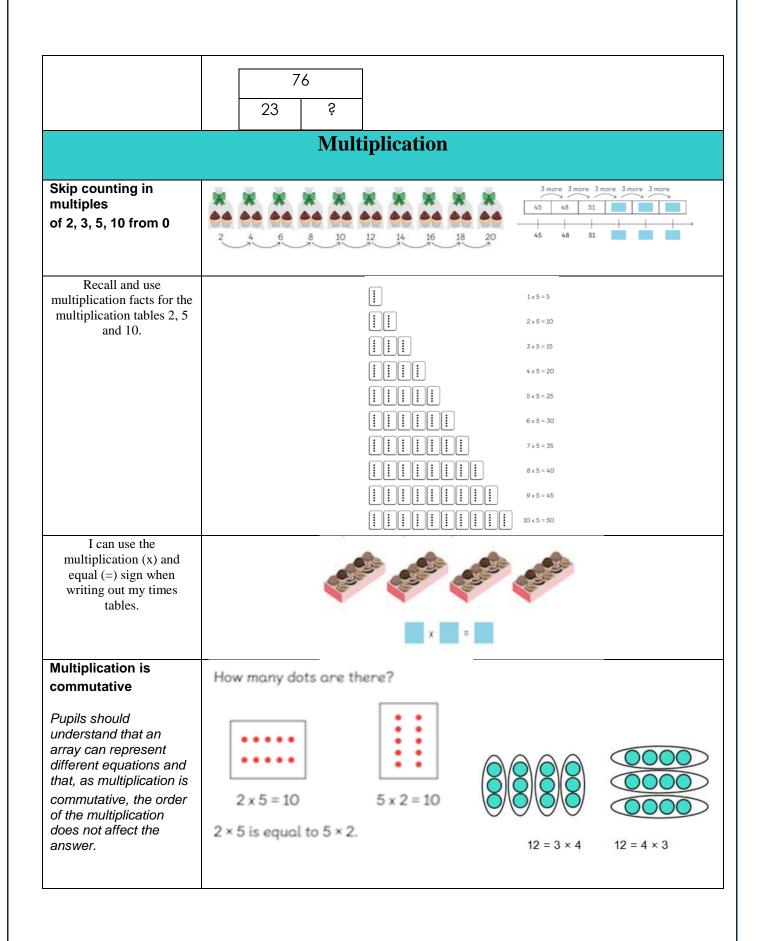
Step 2 Add the tens. 1 ten + 2 tens = 3 tens

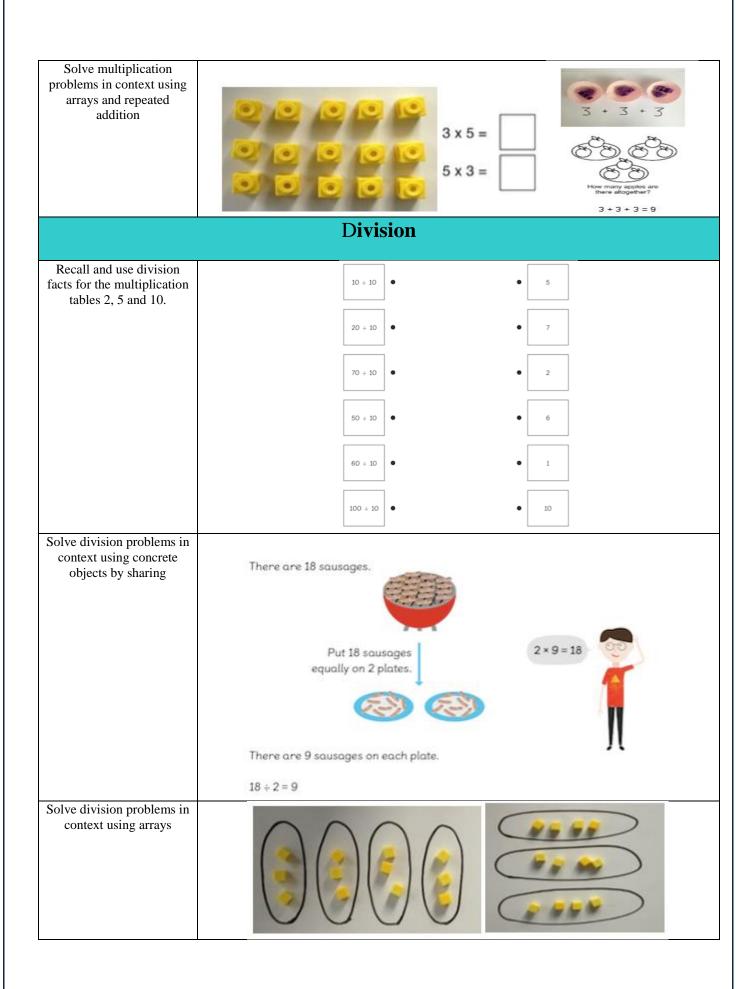


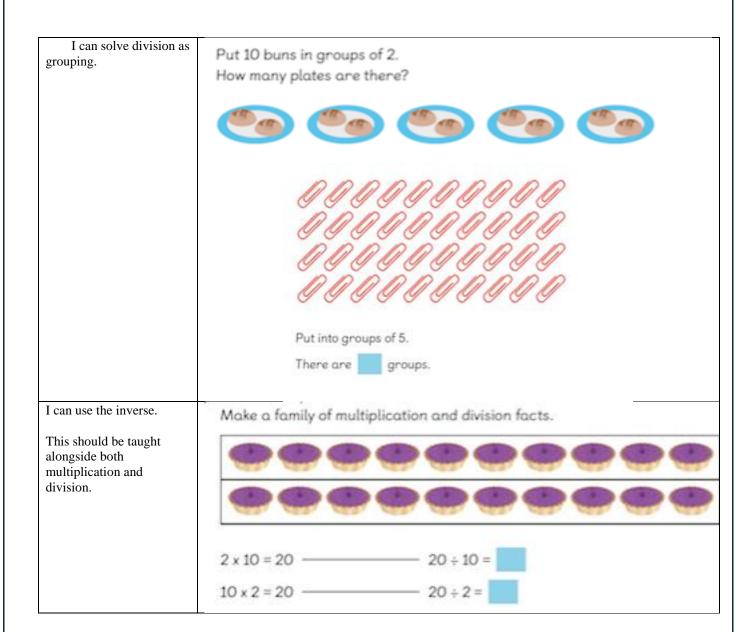
	tens	ones	
	1	9	
+	2	0	
	3	9	

Using concrete objects and Step 2 Add the tens. pictorial representations to 2 tens + 1 ten = 3 tensadd a 2 2 digit numbers. ones tens 2 3 ΘĐ 1 3 23 + 14 = 37Adding with renaming Use to help you add. Add 15 and 18. Step 1 Add the ones. 5 ones + 8 ones = 13 ones Regroup the ones. 13 ones = 1 ten and 3 ones tens ones 1 5 8 1 1 3 Step 2 Add the tens. tens ones 1 ten + 1 ten + 1 ten = 3 tens 5 1 8 1 1 3 2 0 3 3 15 + 18 = 33 Using concrete objects and 7+3+2 = leads to 10 + 2 =pictorial representations to add a 3 single digit numbers. Using the bar to find Helen has 14 breadmissing digits. sticks. Her friend has *It is important for children* 17 17. How many do they 14 to use the bar in this way to encourage the use of it have altogether? to aid with problem solving.

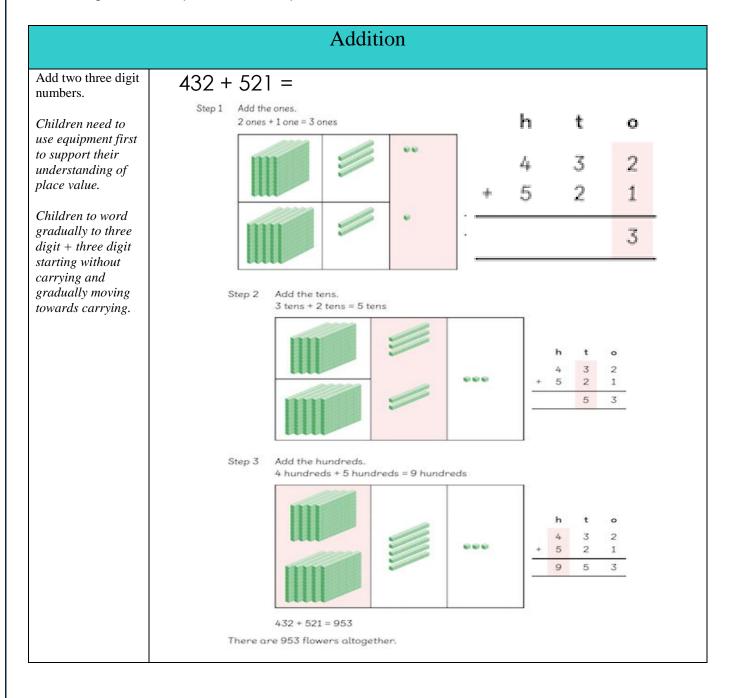


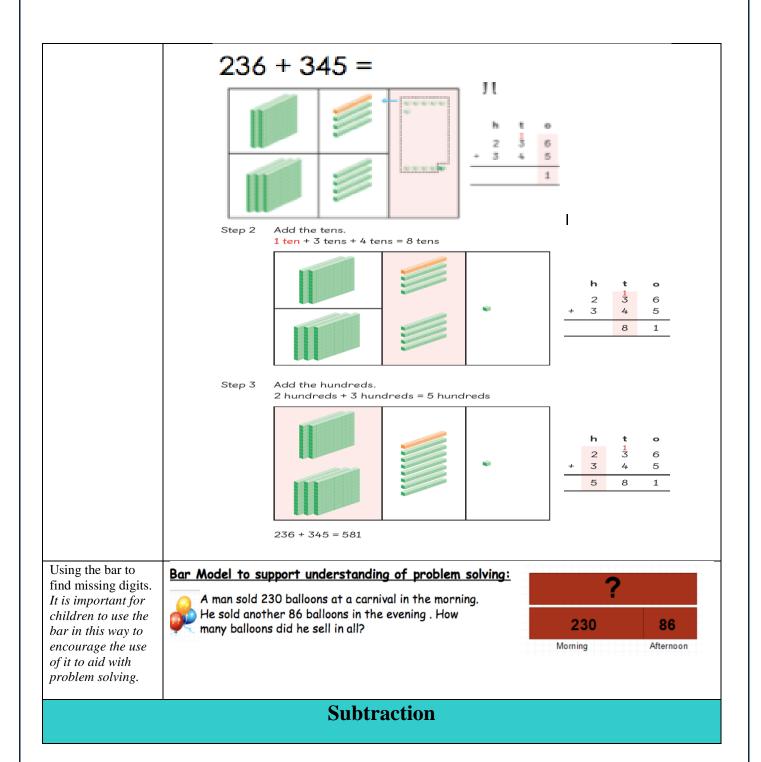






Progression Step 7 – lower Step 8





Only when secure with the method should exchanging be introduced. Subtract up to 3 digits from 3 digits. Step 2 Subtract the tens. 7 tens - 2 tens = 5 tens Very important for children to use dienes equipment along with a place value chart to support. Subtract 723 from 975. Subtract the hundreds. 9 hundreds – 7 hundreds = 2 hundreds Subtract the ones. 5 ones – 3 ones = 2 ones 975 - 723 = 252 Regroup 1 hundred into 10 tens. Subtract the tens. 11 tens - 6 tens = 5 tensSubtract the hundreds. 4 hundreds – 2 hundreds = 2 hundreds 520 - 269 = 251 Subtract 269 from 520. 520 Step 1 Regroup 1 ten into 10 ones. Subtract the ones. 400 110 10 10 ones - 9 ones = 1 one

Using the bar to find missing digits. 315 315 - 185 = ?185 + ? = 315 It is important for ? 185 children to use the bar in this way to encourage the use of it to aid with ? 185 + 315 = ? problem solving. ? - 185 = 315315 185 Multiplication Children should be Let's Learn able to recall the 2, 5, 10, 3, 4 and 8 There are 4 groups of 23 fish. times tables. How do we multiply 23 by 4? Multiple a two-Step 1 Multiply the ones by 4. digit number by a one digit. $4 \text{ ones} \times 3 = 12 \text{ ones}$ 12 ones = 1 ten 2 ones Step 2 Multiply the tens by 4. 2 tens × 4 = 8 tens Add the products. 12 + 80 = 92 23 × 4 = 92 There are 92 fish in 4 tanks. Using the bar to solve Whole unknown 4 children go to the cinema. multiplication They each pay £15. How much problems.

do they spend altogether?

15

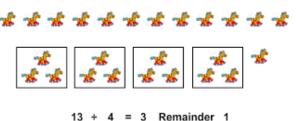
15

15

15

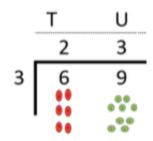
Division

Dividing by grouping understanding the concept of remainders. Start with using the real objects-or objects that represent the calculation.



Dividing using short division.

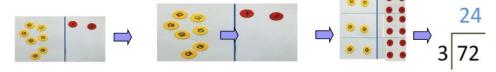
Once children are secure with division as grouping and demonstrate this using number lines, arrays etc., short division for larger 2-digit numbers should be introduced, initially with carefully selected examples requiring no calculating of remainders at all. Start by introducing the layout of short division by comparing it to an array.



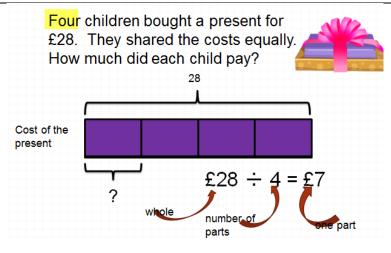
Remind children of correct place value, that 69 is equal to 60 and 9, but in short division, pose:

- · How many 3's in 6? = 2, and record it above the **6 tens**.
- · How many 3's in 9? = 3, and record it above the **9 ones**.

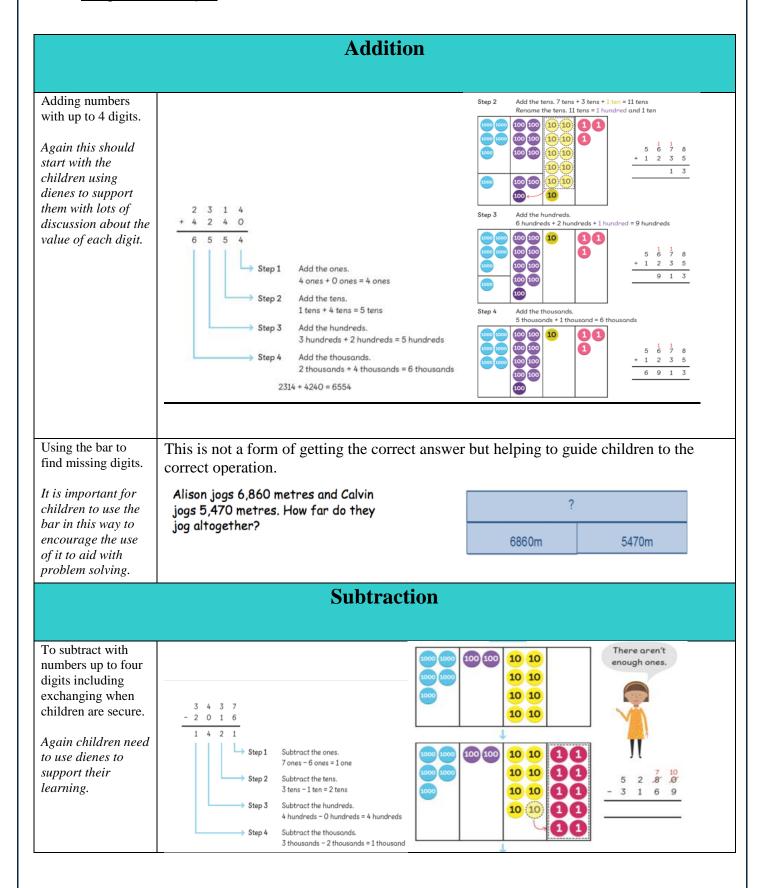
Once children demonstrate a full understanding of remainders, and also the short division method taught, they can be taught how to use the method when remainders occur within the calculation (e.g. $72 \div 3$), and be taught to 'carry' the remainder onto the next digit.

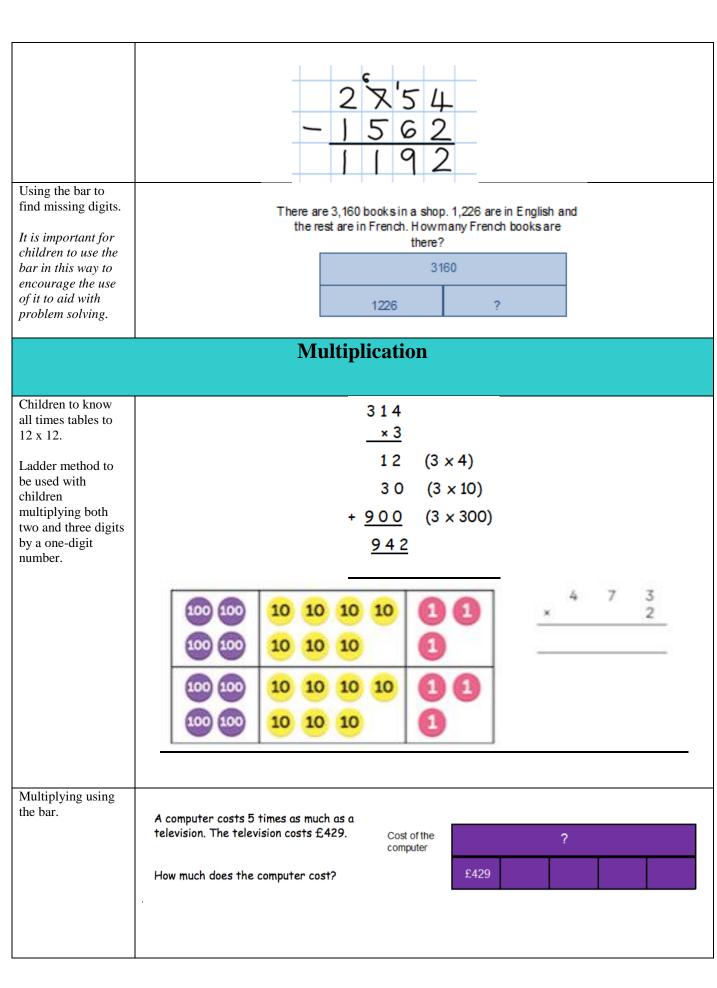


Using the bar to aid the solving of division problems.



Progression Step 8



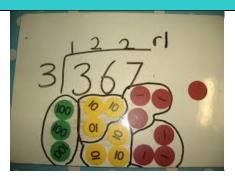


Division

Dividing up to three digit numbers by a one-digit number using short division.

Only when the children are secure with dividing a two-digit number should they move onto a 3-digit number.

Dividing using the bar.

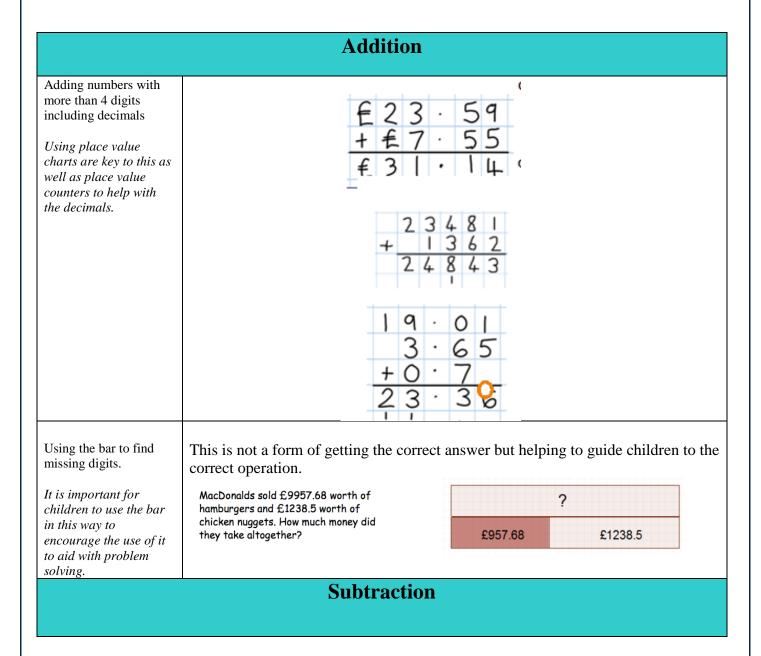


	H 0	T 2	U 5	r1
5	1	12	²6	
		***	***	٠

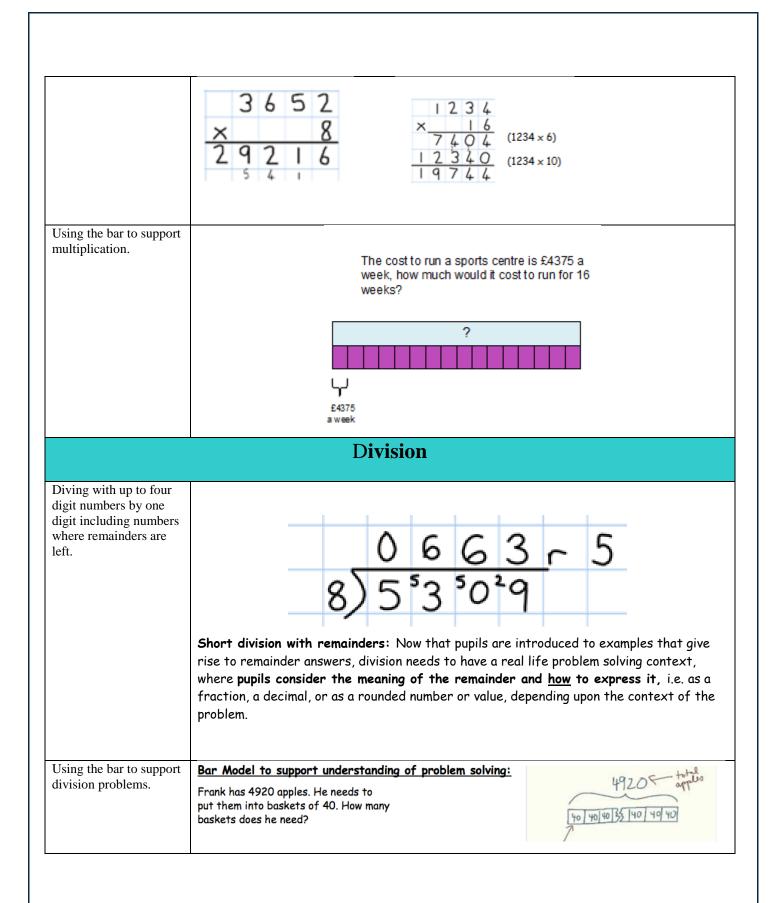
Desmond and Melissa collect cards. They have 192 cards in all. Melissa has three times as many cards as Desmond. How many cards does Desmond have?

192			
D =?	M	M	M

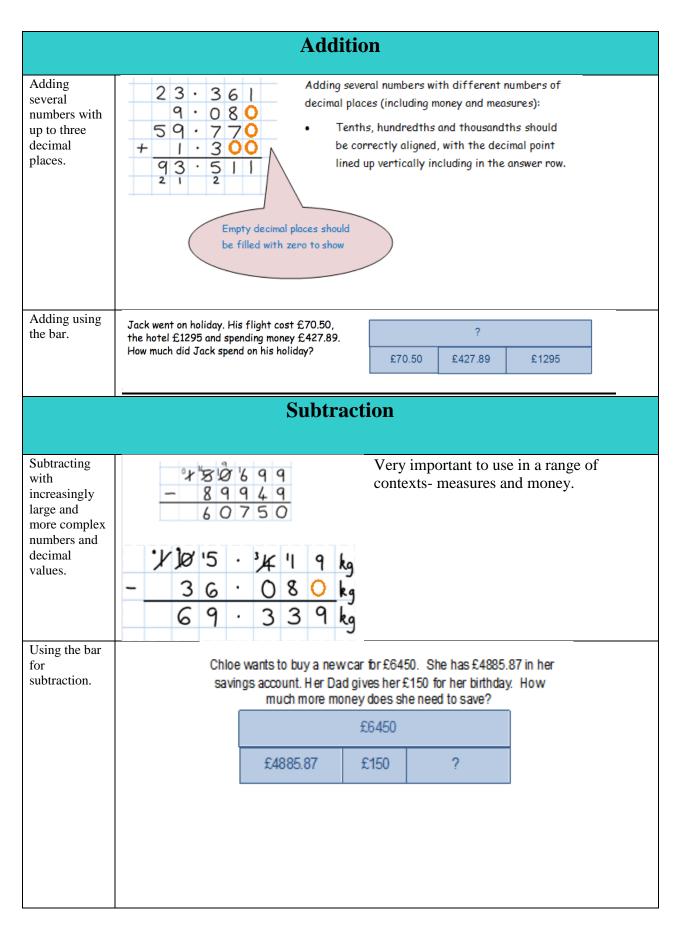
Progression Step 8-lower Step 9

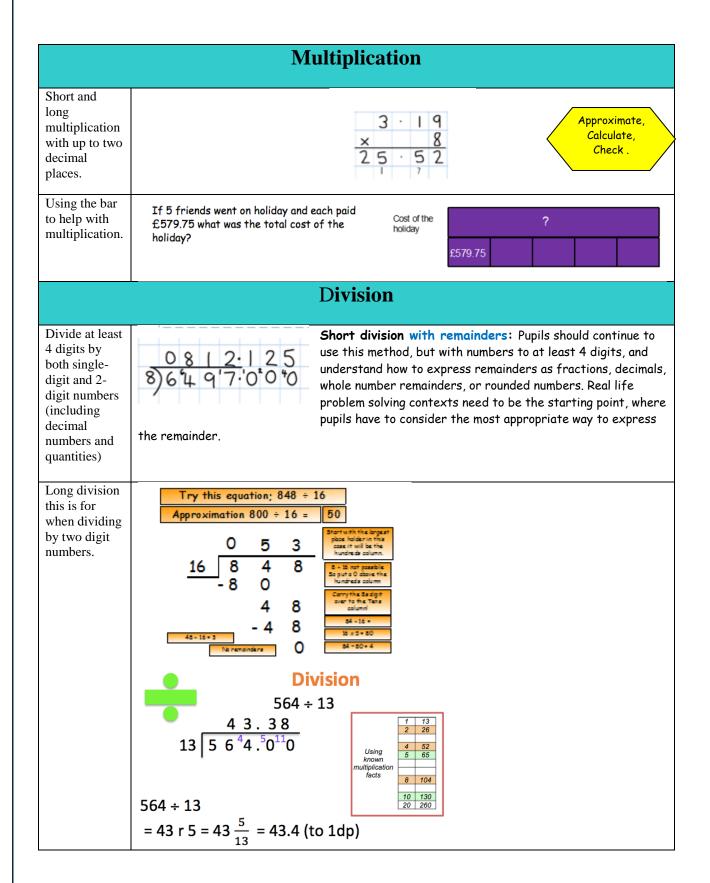


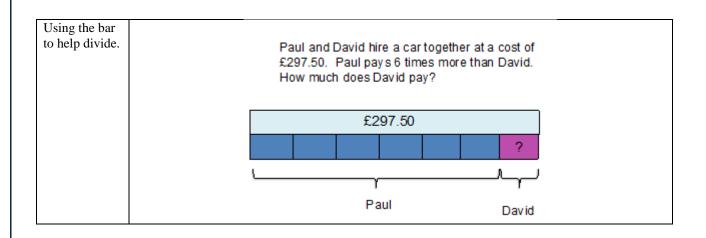
Subtract with at least Subtract with decimal values, including mixtures of integers and four digit numbers decimals, aligning the decimal point. including two decimal places. 18018 Include money, measures and **Approxima** decimals ensuring te, that children do this Calculate, Check. practically before the abstract. Using the bar to find A whole to Lapland costs £5005 for a family of four. missing digits. the Smith's have only saved £3787.75, how much money do they still need to find? It is important for children to use the bar in this way to £5005 encourage the use of it to aid with problem ? £3787.75 solving. Multiplication Multiplying up to four 56 digit numbers by two Approximate, X 27 digits using long Calculate, multiplication. Check. 392 (56x7) Children need to be 1120 (56x20) taught to approximate first, e.g. for 72 x 38, they will use rounding: 1512 72 x 38 is approximately 70 x 40 = **2800**, and use the · Explain that first we are multiplying the top number by 7 starting with the units. approximation to check (any carrying needs to be done underneath the numbers). the reasonableness of · Now explain that we need to put a 0 underneath—explain that this is because we their answer. are multiplying the number by 20.. (2 tens) which is the same as multiplying 10 and 2. · Now add the 2 numbers together to give you the answer. · This will need lots of modeling to show the children.



Progression Step 9







Additional Relevant Documents

Mathematics Policy